## Math Virtual Learning

## Probability and Statistics

## April 23, 2020

Probability and Statistics
Lesson: April 23, 2020

## Objective/Learning Target:

Students will be able to convert $z$-scores into percentages for a set of data

## Let's Get Started!

Women's heights have a mean of 63.6 in . and a standard deviation of 2.5 inches. Find the $z$ score corresponding to a woman with the following heights.
A. Height $=67^{\prime \prime}$
B. $\quad$ Height $=72^{\prime \prime}$
C. Height $=44^{\prime \prime}$
D. What height would be 2 standard deviations below the mean?
E. What height has a z-score of 2.5 (Hint: Work Backwards with the Formula)

## Let's Get Started!

Women's heights have a mean of 63.6 in. and a standard deviation of 2.5 inches. Find the $z$ score corresponding to a woman with the following heights.
A. Height $=67$ " $\quad \frac{67-63.6}{2.5}=1.36$
B. $\quad$ Height $=72^{\prime \prime} \quad \frac{72-63.6}{2.5}=3.36$
C. Height $=58$ " $\frac{58-63.6}{2.5}=-2.24$
D. What height would be 2 standard deviations below the mean? 58.6 inches
E. What height has a z-score of 2.5 (Hint: Work Backwards with the Formula)

$$
\begin{array}{rll}
2.5=\frac{x-63.6}{2.5} & ---->6.25=x-63.6 & \text { (multiply both sides by 2.5) } \\
& ---->x=69.85 \text { in. } & \text { (add } 63.6 \text { to both sides) }
\end{array}
$$

## What we already know...

Now that we know how to calculate a Z-Score using the formula

AND we know how to put that answer onto the graph:


## Z-Score to Percent...

Now we can answer questions about percentages using a Z-Score to Percent Chart

You will want to open or print this chart for referencing during this lesson

## Z-Score to Percent Chart

The first thing you will notice is that there are 2 charts. One has negative values and the other has positive values.

When your Z-Score is above the Mean you will use the positive chart

When your Z-Score is below the Man you will use the negative chart

## Let's start with the first example from the Bell Ringer...

Women's heights have a mean of 63.6 in . and a standard deviation of 2.5 inches. Find the $z$ score corresponding to a woman with the following heights.

$$
\text { A. } \quad \text { Height }=67^{\prime \prime} \quad \frac{67-63.6}{2.5}=1.36
$$

We want to know what percent of the women surveyed have a height of 67" or less
(We know that it will be more than $50 \%$ because the Z-Score (1.36) is on the right side of the mean since it is a positive Z-Score.)

To find the exact \%, take your Z-Score (1.36) and look it up on the Z-Score to Percent Chart that I told you to open or print from Slide 6

Here it is again for you: Z-Score to Percent Chart
Watch this short video on how to read/use the chart to find your percentage answer:

## Reading a Z-Score to Percent Chart

## Let's start with the first example from the Bell Ringer...

Women's heights have a mean of 63.6 in . and a standard deviation of 2.5 inches. Find the z score corresponding to a woman with the following heights.
A. Height $=67$ "


| $\mathbf{z}$ | $\mathbf{0 . 0 0}$ | $\mathbf{0 . 0 1}$ | $\mathbf{0 . 0 2}$ | $\mathbf{0 . 0 3}$ | $\mathbf{0 . 0 4}$ | $\mathbf{0 . 0 5}$ | 0.06 | 0.07 | $\mathbf{0 . 0 8}$ | $\mathbf{0 . 0 9}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{0 . 0}$ | .5000 | .5040 | .5080 | .5120 | .5160 | .5199 | .5239 | .5279 | .5319 | .5359 |
| $\mathbf{0 . 1}$ | .5398 | .5438 | .5478 | .5517 | .5557 | .5596 | .5636 | .5675 | .5714 | .5753 |
| $\mathbf{0 . 2}$ | .5793 | .5832 | .5871 | .5910 | .5948 | .5987 | .6026 | .6064 | .6103 | .6141 |
| $\mathbf{0 . 3}$ | .6179 | .6217 | .6255 | .6293 | .6331 | .6368 | .6406 | .6443 | .6480 | .6517 |
| $\mathbf{0 . 4}$ | .6554 | .6591 | .6628 | .6664 | .6700 | .6736 | .6772 | .6808 | .6844 | .6879 |
| $\mathbf{0 . 5}$ | .6915 | .6950 | .6985 | .7019 | .7054 | .7088 | .7123 | .7157 | .7190 | .7224 |
| $\mathbf{0 . 6}$ | .7257 | .7291 | .7324 | .7357 | .7389 | .7422 | .7454 | .7486 | .7517 | .7549 |
| $\mathbf{0 . 7}$ | .7580 | .7611 | .7642 | .7673 | .7704 | .7734 | .7764 | .7794 | .7823 | .7852 |
| $\mathbf{0 . 8}$ | .7881 | .7910 | .7939 | .7967 | .7995 | .8023 | .8051 | .8078 | .8106 | .8133 |
| $\mathbf{0 . 9}$ | .8159 | .8186 | .8212 | .8238 | .8264 | .8289 | .8315 | .8340 | .8365 | .8389 |
| $\mathbf{1 . 0}$ | .8413 | .8438 | .8461 | .8485 | .8508 | .8531 | .8554 | .8577 | .8599 | .8621 |
| $\mathbf{1 . 1}$ | .8643 | .8665 | .8686 | .8708 | .8729 | .8749 | .8770 | .8790 | .8810 | .8830 |
| $\mathbf{1 . 2}$ | .8849 | .8869 | .8888 | .8907 | .8925 | .8944 | 8962 | .8980 | .8997 | .9015 |
| $\mathbf{1 . 3}$ | .9032 | .9049 | .9066 | .9082 | .9099 | .9115 | .9131 | .9147 | .9162 | .9177 |
| $\mathbf{1 . 4}$ | .9192 | .9207 | .9222 | .9236 | .9251 | .9265 | .9279 | .9292 | .9306 | .9319 |
| $\mathbf{1 . 5}$ | .9332 | .9345 | .9357 | .9370 | .9382 | .9394 | .9406 | .9418 | .9429 | .9441 |
| $\mathbf{1 . 6}$ | .9452 | .9463 | .9474 | .9484 | .9495 | .9505 | .9515 | .9525 | .9535 | .9545 |

***Keep in mind that the chart AIWAYS gives you the \% on the left or the \% LOWER than your data point. This is very important to remember when using this chart!

## Let＇s do Example 2 from the Bell Ringer．．．

Women＇s heights have a mean of 63.6 in ．and a standard deviation of 2.5 inches．Find the z score corresponding to a woman with the following heights．
B． Height $=72^{\prime \prime} \quad \frac{72-63.6}{2.5}=3.36$
Find the \％of women shorter than 72＂
From the chart，we get .9996 or $99.96 \%$（so almost everyone is shorter than 72 in ．）

So what \％of the women are taller than 72＂

| $z$ | 0.0 | 0.91 | 000 | 4 mm | 404 | 408 | 408 | 0.97 | 028 | 0.08 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 00 | 5000 | 5010 | 5000 | 5120 | 5150 | 5739 | 5208 | 508 | 5019 | $5 \times 5$ |
| 0.1 | 5598 | 5438 | 5478 | ． 5517 | 5557 | 5936 | 535 | 5605 | 5014 | 5053 |
| 02 | 5935 | 5882 | 5871 | 5970 | 5548 | 5387 | 8006 | 6064 | ¢123 | （14） |
| 03 | 6173 | k21］ | 5235 | A23 | 4371 | 483 | 300 | ${ }^{864} 4$ | 840 | ${ }^{6817}$ |
| 0.4 | 594 | 3081 | $4{ }^{488}$ | 10654 | kw | A ${ }^{5}$ | 研 72 | 8608 | 504 | H39 |
| 0.5 | 5015 | ${ }^{6350}$ | 6585 | ． 7019 | 3054 | 338 | ． 7123 | T15 | 7130 | 3224 |
| 0.6 | 3257 | ． 2381 | 3324 | ．357 | 339 | 242 | ．7154 | 7688 | 3517 | 3549 |
| 0.7 | 358 | 3611 | 382 | 383 | 734 |  | 7ns4 | ग\％ | 32 | 385 |
| 08 | נ\％ | ． 810 | 3 m | 337 | 305 | \＄103 | \％${ }^{0}$ | 808 | 11\％ | 818 |
| 09 | 8159 | 8158 | 1812 | ．3238 | 2254 | 2333 | 8315 | 8340 | 1395 | 8859 |
| 1.0 | ${ }^{6} 413$ | 8438 | 8461 | 3465 | ${ }^{2558}$ | 8531 | ${ }^{83} 8$ | 857 | 8599 | 8621 |
| 1.1 | 864 | 3＊5 | 4688 | 3708 | 473 |  | 370 | 8050 | 885 | 4838 |
| 12 | （649 | 楼 | 888 | 337 | 825 | 234 | 解 | \％ 86 | 399 | S015 |
| 13 | 5092 | 5049 | ． 5055 | 3082 | 5089 | ． 315 | 9131 | 9147 | 9052 | 917 |
| 1.4 | ． 9192 | 5000 | ． 5232 | 2935 | 9251 | 3305 | 9279 | 9058 | 5938 | 5979 |
| 15 | ． 9022 | Sen 5 | 5357 | 330 | 5302 | 334 | 900 | 9718 | 5423 | 5441 |
| 15 | ．958 | 206 | ． 8984 | 3085 | \＄458 | \＄205 | \＄815 | sks | S63 | \＄845 |
| 1.7 | 5854 | Sces | ． 9573 | ． 3532 | 9591 | ． 3599 | ．9508 | S61E | 9625 | 5638 |
| 18 | 5641 | 9645 | 5656 | ．3054 | 9671 | 3078 | ． 9508 | 9685 | Se93 | 5906 |
| 19 | 9713 | 975 | 5728 | ．338 | ． 9338 | 3244 | 9350 | 9158 | 5381 | 909 |
| 20 | 972 | 971 | 508 | 小3 | 508 | 731 | sw | Ste | 4012 | H017 |
| 21 | 5621 | Stas | 5830 | 3834 | 5838 | ． 3802 | 388 | 9650 | ． 3654 | Sts |
| 22 | 5651 | 5684 | 5858 | ． 9871 | 5875 | 3878 | 9881 | 5684 | 5897 | Seso |
| 23 | 5 ses | Sese | 5e38 | 4301 | 5504 | 3598 | 200 | S011 | 5943 | S678 |
| 24 | \＄614 | sax | \＄022 | ＊35 | \＄627 | \＄120 | 3s31 | \＄802 | ． 183 | 8008 |
| 25 | 5588 | 980 | ． 9941 | 3943 | 5945 | 3955 | 9948 | 994 | 9951 | 955 |
| 26 | 9551 | 9555 | 9956 | ． 9357 | ． 9859 | 4950 | ．9361 | 9662 | 5963 | 9664 |
| 2.7 | 9865 | 9688 | 9807 | ， 3 30 | \＄869 | ． 2970 | 2971 | 9002 | 5973 | ． 9894 |
| 21 | \＄934 | sans | Sus | m\％ | san | स冈 | ＊\％9 | 909 | ． 510 | 864 |
| 29 | 5681 | 5602 | 5982 | 938 | S904 | 3394 | 9955 | 965 | 5935 | 5665 |
| 3.0 | 5967 | 5581 | 9987 | ． 9338 | 5s89 | 2394 | 9369 | 9599 | 5939 | 5980 |
| 3.1 | \＄550 | Sest | 9931 | 3331 | 5932 | 392 | 9mp | 9685 | 923 | 9653 |
| 12 |  | \＄600 | 5094 | mas | \＄064 | 1 mb | ＊＊ | 905 | 5035 | \＄05s |
| 13 | 9695 | 9908 | 9995 | 3935 | 9986 | －10． | 3936 | 9585 | 5996 | ．5067 |
| 3.4 | 9887 | 9881 | 98 | 99 | 5989 |  | 9997 | gess | 9937 | 9688 |


$100 \%-99.96 \%($ shorter $)=.04 \%$（taller） | 3.2 | .9993 | .9993 | .9994 | .9994 |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 3.3 | .9995 | .9995 | .9995 | .9996 |  |
|  | 3.4 | .9997 | .9997 | .9997 | .9997 |

## Now let's combine Part A and Part B for a new

 question:Women's heights have a mean of 63.6 in . and a standard deviation of 2.5 inches. Find the z score corresponding to a woman with the following heights.
A. Height $=67 \prime \quad \frac{67-63.6}{2.5}=1.36 \quad 91.31 \%$ shorter
B. Height $=72 " \frac{72-63.6}{2.5}=3.36 \quad 99.96 \%$ shorter

What \% of women are BETWEEN 67" and 72"?


We only care about the \% between 67 and 72, so we need to subtract the double shaded area (\%).

### 8.65\% ----------------------->

## Your turn...

Women's heights have a mean of 63.6 in . and a standard deviation of 2.5 inches. Find the z score corresponding to a woman with the following height.
C. Height $=58$ "

1. What $\%$ of women are shorter than 58 "
2. What $\%$ of women are taller than 58 "
3. What \% of women are between $58^{\prime \prime}$ and $67^{\prime \prime}$

## Your turn...

Women's heights have a mean of 63.6 in . and a standard deviation of 2.5 inches. Find the z score corresponding to a woman with the following heights.
C. Height $=58$ " Z-Score $=-2.24 \quad$ (Remember to use the negative side of the chart)

1. What $\%$ of women are shorter than 58 "
2. What \% of women are taller than 58 "
3. What $\%$ of women are between 58 " and 67 "
.0125 (from chart) $=1.25 \%$ 100\%-1.25\% = 98.75\%

| $91.31 \%-$ | $1.25 \%=$ | $90.06 \%$ |
| :---: | :---: | :---: |
| $67 \% \%$ | $58 \% \%$ | $\%$ <br> Between <br> 58 and 67 |

